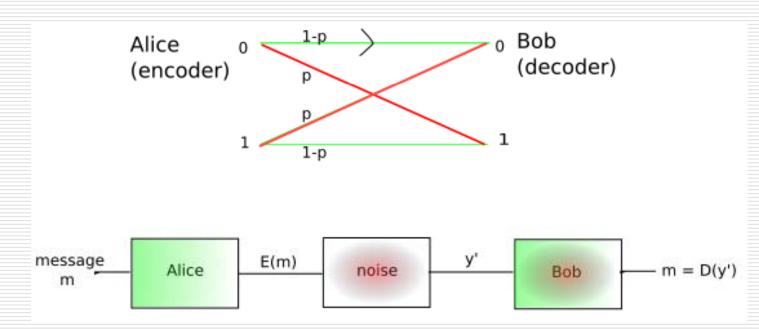
Channel Coding

Recap...

- Information is transmitted through channels (eg. Wires, optical fibres and even air)
- Channels are noisy and we do not receive what was transmitted

System Model

A Binary Symmetric Channel



Crossover with probability p

Repetition Coding

□ Assume 1/3 repetition $0 \rightarrow 000$ □ What is the probability of $1 \rightarrow 111$ error ?

$$P_e = {}^{3}C_2 p^2 (1-p) + p^3$$

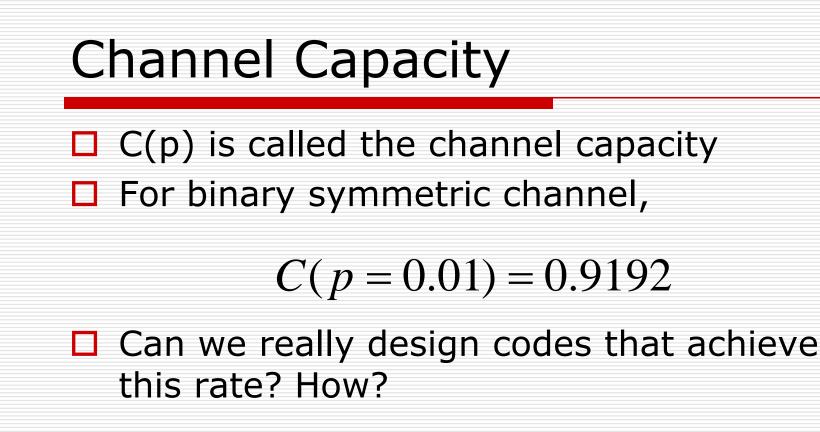
- □ If crossover probability p = 0.01, Pe \approx 0.0003
- Here coding rate R = 1/3. Can we do better? How much better?

Shannon's Theorem

- 🗆 Given,
 - A noisy channel (some fixed p)
 - A value of Pe which we want to achieve

"We can transmit through the channel and achieve this probability of error at a maximum coding rate of C(p)"

- □ Is it counterintuitive?
- Do such good codes exist?



Parity Check Codes

□ #information bits transmitted = k □ #bits actually transmitted = n = k+1 □ Code Rate R = k/n = k/(k+1)

Error detecting capability = 1
 Error correcting capability = 0

2-D Parity Check

Rate?
Error detecting
capability?
Error correcting
capability?

 1
 0
 1
 0

 0
 1
 0
 0
 1

 1
 0
 0
 1
 Last column consists of check bits for each

 1
 1
 0
 1
 1

 1
 0
 1
 1
 0

 1
 0
 1
 1
 0

 1
 0
 1
 1
 1

Bottom row consists of check bit for each column

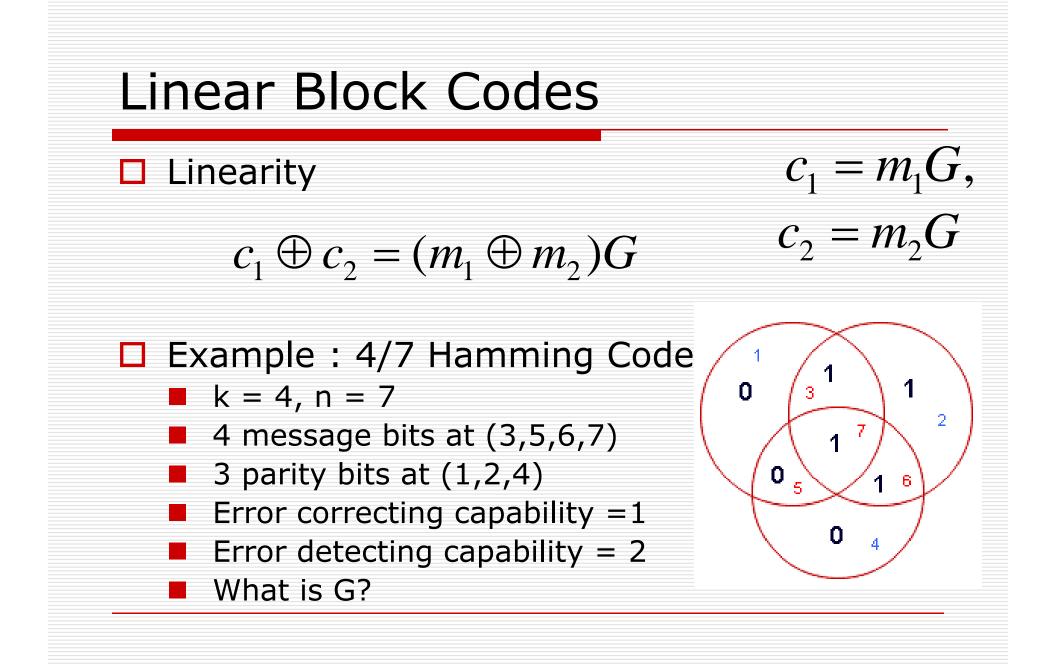
Linear Block Codes

- #parity bits n-k (=1 for Parity Check)
- $\square Message m = \{m_1 m_2 \dots m_k\}$
- □ Transmitted Codeword $c = \{c_1 \ c_2 \ ... \ c_n\}$

A generator matrix G_{kxn}

$$c = mG$$

What is G for repetition code?For parity check code?



Cyclic codes

- Special case of Linear Block Codes
- Cyclic shift of a codeword is also a codeword
 - Easy to encode and decode,
 - Can correct continuous bursts of errors
 - CRC (used in Wireless LANs), BCH codes, Hamming Codes, Reed Solomon Codes (used in CDs)

Convolutional Codes Block codes require a buffer What if data is available serially bit by bit? Convolutional Codes Example k = 1n = 2x⁽¹⁾ D D Rate R = $\frac{1}{2}$

Convolutional Codes

- Encoder consists of shift registers forming a finite state machine
- Decoding is also simple Viterbi Decoder which works by tracking these states
- First used by NASA in the voyager space programme
- Extensively used in coding speech data in mobile phones

Achieving Capacity

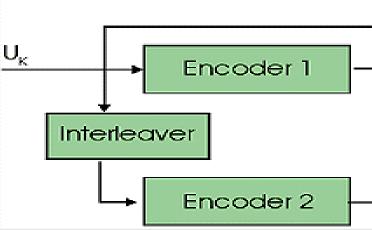
Do Block codes and Convolutional codes achieve Shannon Capacity?

Actually they are far away

- Achieving Capacity requires large k (block lengths)
- Decoder complexity for both codes increases exponentially with k – not feasible to implement

Turbo Codes

- Proposed by Berrou & Glavieux in 1993
- Advantages



 X_{ν}

- Use very large block lengths
- Have feasible decoding complexity
- Perform very close to capacity
- Limitation delay, complexity

Summary

- There is a limit on the how good codes can be
- Linear Block Codes and Convolutional Codes have traditionally been used for error detection and correction
- Turbo codes in 1993 introduced a new way of designing very good codes with feasible decoding complexity